# Mathematics & Statistics (MATH)

- Course numbers with the # symbol included (e.g. #400) have not been taught in the last 3 years.

**MATH 801 - Exploring Mathematics for Teachers I**
**Credits:** 3
Provides prospective elementary teachers with the opportunity to explore and master concepts involving number systems and operations, data analysis and probability. Additional topics may include geometry, measurement, and algebraic thinking. Mathematical reasoning, problem solving, and the use of appropriate manipulatives and technology are integrated throughout the course. Readings, class discussions, and assignments focus on mathematics content as well as applicable theories of learning, curriculum resources, and state and national recommendations. The course models instructional techniques that can be adapted to the elementary curricula. Credit offered only to M.Ed. and M.A.T., certificate students, and in-service teachers. (Not offered for credit if credit is received for MATH 821 or MATH 823.)

**Prerequisite(s):** (EDUC 500 with a minimum grade of D- or EDUC 935 with a minimum grade of B-).

**Equivalent(s):** MATH 601, MATH 821, MATH 823

**MATH 821 - Number Systems for Teachers**
**Credits:** 3
Ways of representing numbers, relationships between numbers, number systems, the meanings of operations and how they relate to one another, and computation with number systems as a foundation for algebra; episodes in history and development of the number system; and examination of the developmental sequence and learning trajectory as children learn number concepts. Credit offered only to M.Ed., M.A.T., Elementary Math Specialist certificate only students, and in-service teachers. Not offered for credit if credit received for MATH 621.

**Equivalent(s):** MATH 621

**MATH 823 - Statistics and Probability for Teachers**
**Credits:** 3
An introduction to probability, descriptive statistics and data analysis; exploration of randomness, data representation and modeling. Descriptive statistics will include measures of central tendency, dispersion, distributions and regression. Analysis of experiments requiring hypothesizing, experimental design and data gathering. Credit offered only to M.Ed., M.A.T., Elementary Math Specialist certificate only students, and in-service teachers. Not offered for credit if credit received for MATH 623.

**Prerequisite(s):** (MATH 621 with a minimum grade of D- or MATH 821 with a minimum grade of B-).

**Equivalent(s):** MATH 621

**MATH 825 - Algebra and Functions for K-8 Mathematics Teachers**
**Credits:** 3
Representation and analysis of mathematical structures using generalization and algebraic symbols and reasoning. Attention is given to transition from arithmetic to algebra, working with quantitative change, the description of and prediction of change, and concepts in discrete mathematics.

**Prerequisite(s):** (MATH 621 with a minimum grade of D- or MATH 821 with a minimum grade of B-).

**Equivalent(s):** MATH 625

**MATH 831 - Mathematics for Geodesy**
**Credits:** 3
A survey of topics from undergraduate mathematics designed for graduate students in engineering and science interested in applications to geodesy and Earth Sciences. Topics include essential elements from analytic geometry, geometry of surfaces, linear algebra and statistics, Fourier analysis, discrete Fourier transforms and software, filtering applications to tidal data.

**Prerequisite(s):** (MATH 645 with a minimum grade of D- or MATH 645H with a minimum grade of D- or MATH 762 with a minimum grade of D- or MATH 862 with a minimum grade of B-).

**MATH 835 - Statistical Methods for Research**
**Credits:** 3
This course provides a solid grounding in modern applications of statistics to a wide range of disciplines by providing an overview of the fundamental concepts of statistical inference and analysis, including t-tests and confidence intervals. Additional topics include: ANOVA, multiple linear regression, analysis of cross classified categorical data, logistic regression, nonparametric statistics and data mining using CART. The use of statistical software, such as JMP, S PLUS, or R, is fully integrated into the course.

**Prerequisite(s):** (MATH 835 with a minimum grade of B- or MATH 839 with a minimum grade of B-).

**MATH 836 - Advanced Statistical Methods for Research**
**Credits:** 3
An introduction to multivariate statistical methods, including principal components, discriminant analysis, cluster analysis, factor analysis, multidimensional scaling, and MANOVA. Additional topics include generalized linear models, general additive models, depending on the interests of class participants. This course completes a solid grounding in modern applications of statistics used in most research applications. The use of statistical software, such as JMP, S PLUS, or R, is fully integrated into the course.

**Prerequisite(s):** (MATH 835 with a minimum grade of B- or MATH 839 with a minimum grade of B-).

**MATH 837 - Statistical Methods for Quality Improvement and Design**
**Credits:** 3
Six Sigma is a popular, data-focused methodology used worldwide by organizations to achieve continuous improvement of their existing processes, products and services or to design new ones. This course provides a thorough introduction to the Six Sigma principles, methods, and applications for continuous improvement (DMAIC process) and an overview of Design for Six Sigma (DFSS). Both manufacturing and non-manufacturing (transactional Six Sigma) applications will be included. Emphasis is placed on the use of case studies to motivate the use of, as well as the proper application of, the Six Sigma methodology. Formal Six Sigma Green Belt certification from UNH may be attained by successfully completing TECH 696. Students must have completed a calculus-based introductory statistics course.
MATH 835 - Time Series Analysis
Credits: 3
An introduction to univariate time series models and associated methods of data analysis and inference in the time domain and frequency domain. Topics include: Auto regressive (AR), moving average (MA), ARMA and ARIMA processes, stationary and non-stationary processes, seasonal ARIMA processes, auto-correlation and partial auto-correlation functions, identification of models, estimation of parameters, diagnostic checking of fitted models, forecasting, spectral density function, periodogram and discrete Fourier transform, linear filters. parametric spectral estimation, dynamic Fourier analysis. Additional topics may include wavelets and long memory processes (FARIMA) and GARCH Models. The use of statistical software, such as JMP, or R, is fully integrated in to the course. Offered in alternate years in the spring. **Prerequisite(s):** MATH 835 with a minimum grade of B- or MATH 839 with a minimum grade of B-.

MATH 840 - Design of Experiments II
Credits: 3
Second course in design of experiments, with applications in quality improvement and industrial manufacturing, engineering research and development, research in physical and biological sciences. Covers experimental design strategies and issues that are often encountered in practice complete and incomplete blocking, partially balanced incomplete blocking (PBIB), partial confounding, intra and inter block information, split plotting and strip plotting, repeated measures, crossover designs, Latin squares and rectangles, Youden squares, crossed and nested treatment structures, variance components, mixed effects models, analysis of covariance, optimizations, space filling designs, and modern screening design strategies. **Prerequisite(s):** MATH 840 with a minimum grade of B-.

MATH 841 - Survival Analysis
Credits: 3
Explorations of models and data-analytic methods used in medical, biological, and reliability studies. Event-time data, censored data, reliability models and methods, Kaplan-Meier estimator, proportional hazards, Poisson models, loglinear models. The use of statistical software, such as SAS, JMP, or R, is fully integrated into the course. Prereq: MATH 839. (Offered in alternate years.)

MATH 842 - Foundations of Applied Mathematics II
Credits: 3
An introduction to Partial Differential Equations (PDEs) and associated mathematical methods and the analytical foundation for applied mathematics. Topics include: PDE classification, superposition, separation of variables, orthonormal functions, completeness, convergence, Fourier Series, Sturm-Liouville eigenvalue problems, and eigenfunctions. Methods are introduced for the analysis and solution of boundary value problems, in particular, the Heat, Wave, and Laplace equations. Students are required to have a mastery of differential equations and ordinary differential equations. **Prerequisite(s):** MATH 841.

MATH 843 - Time Series Analysis
Credits: 3
An introduction to univariate time series models and associated methods of data analysis and inference in the time domain and frequency domain. Topics include: Auto regressive (AR), moving average (MA), ARMA and ARIMA processes, stationary and non-stationary processes, seasonal ARIMA processes, auto-correlation and partial auto-correlation functions, identification of models, estimation of parameters, diagnostic checking of fitted models, forecasting, spectral density function, periodogram and discrete Fourier transform, linear filters. parametric spectral estimation, dynamic Fourier analysis. Additional topics may include wavelets and long memory processes (FARIMA) and GARCH Models. The use of statistical software, such as JMP, or R, is fully integrated in to the course. Offered in alternate years in the spring. **Prerequisite(s):** MATH 835 with a minimum grade of B- or MATH 839 with a minimum grade of B-.

MATH 844 - Design of Experiments II
Credits: 3
Second course in design of experiments, with applications in quality improvement and industrial manufacturing, engineering research and development, research in physical and biological sciences. Covers experimental design strategies and issues that are often encountered in practice complete and incomplete blocking, partially balanced incomplete blocking (PBIB), partial confounding, intra and inter block information, split plotting and strip plotting, repeated measures, crossover designs, Latin squares and rectangles, Youden squares, crossed and nested treatment structures, variance components, mixed effects models, analysis of covariance, optimizations, space filling designs, and modern screening design strategies. **Prerequisite(s):** MATH 840 with a minimum grade of B-.

MATH 845 - Foundations of Applied Mathematics I
Credits: 3
An introduction to Partial Differential Equations (PDEs) and associated mathematical methods and the analytical foundation for applied mathematics. Topics include: PDE classification, superposition, separation of variables, orthonormal functions, completeness, convergence, Fourier Series, Sturm-Liouville eigenvalue problems, and eigenfunctions. Methods are introduced for the analysis and solution of boundary value problems, in particular, the Heat, Wave, and Laplace equations. Students are required to have a mastery of differential equations and ordinary differential equations. **Prerequisite(s):** MATH 841.

MATH 846 - Foundations of Applied Mathematics II
Credits: 3
An introduction to Partial Differential Equations (PDEs) and associated mathematical methods and the analytical foundation for applied mathematics. Topics include: PDE classification, superposition, separation of variables, orthonormal functions, completeness, convergence, Fourier Series, Sturm-Liouville eigenvalue problems, and eigenfunctions. Methods are introduced for the analysis and solution of boundary value problems, in particular, the Heat, Wave, and Laplace equations. Students are required to have a mastery of differential equations and ordinary differential equations. **Prerequisite(s):** MATH 841.

MATH 847 - Introduction to Nonlinear Dynamics and Chaos
Credits: 3
An introduction to the mathematics of chaos and nonlinear dynamics. Topics include: linear and nonlinear systems of ordinary differential equations; discrete maps; chaos; phase plane analysis; bifurcations; and computer simulations. Prereq: elementary differential equations; linear algebra; and multidimensional calculus. (Not offered every year.)
MATH 853 - Introduction to Numerical Methods
Credits: 3
Introduction to mathematical algorithms and methods of approximation. A wide survey of approximation methods are examined including, but not limited to, polynomial interpolation, root finding, numerical integration, approximation of differential equations, and techniques used in conjunction with linear systems. Included in each case is a study of the accuracy and stability of a given technique, as well as its efficiency and complexity. It is assumed that the student is familiar and comfortable with programming a high-level computer language. (Also offered as CS 853.)
Equivalent(s): CS 853

MATH 855 - Probability with Applications
Credits: 3
Introduces the theory, methods, and applications of randomness and random processes. Probability concepts, random variable, expectation, discrete and continuous probability distributions, joint distributions, conditional distributions; moment-generating functions, convergence of random variables.

MATH 856 - Principles of Statistical Inference
Credits: 3
Introduces the basic principles and methods of statistical estimation and model fitting. One- and two-sample procedures, consistency and efficiency, likelihood methods, confidence regions, significance testing, Bayesian inference, nonparametric and re-sampling methods, decision theory.
Prerequisite(s): MATH 855 with a minimum grade of B-.

MATH 857 - Mathematical Optimization for Applications
Credits: 3
This course introduces the foundations of mathematical optimization and reinforces them via applications. The content includes convex optimization, first and second-order methods, constrained problems, duality, linear and quadratic programming, as well as discrete and non-convex optimization. Applications will focus on machine learning methods but also include problems from engineering and operations research. Students are required to have programming proficiency in MATLAB, R, Java, C, Python, and mastery of Calculus II.
Equivalent(s): CS 857

MATH 859 - Introduction to the R software
Credits: 1
This course provides a basic introduction to the open-source statistical software R for students who have never used this software or have never formally learned the basics of it. Topics include: Numeric calculations, simple and advanced graphics, object management and work-flow, RStudio, user-contributed packages, basic programming, writing of functions, statistical modeling and related graphs, distributed computing, reproducible research and document production via markup language. Cr/F.

MATH 861 - Abstract Algebra
Credits: 3
This course establishes the axiomatic framework that underlies number systems and similar mathematical structures, investigating basic properties of groups, rings, fields and their homomorphisms.

MATH 863 - Abstract Algebra II
Credits: 3
This course extends the investigations of MATH 861 into more specialized situations related to old and new problems in mathematics, such as the nature of solutions of polynomial equations. It presents advanced properties of groups, rings, fields and their applications.
Prerequisite(s): MATH 861 with a minimum grade of B-.

MATH 865 - Introduction to Commutative Algebra and Algebraic Geometry
Credits: 3
Methods of determining solution sets of polynomial systems; affine varieties and their ideals; the 'algebra-geometry correspondence'; theory and applications of Grobner bases.

MATH 867 - One-Dimensional Real Analysis
Credits: 3
Theory of limits, continuity, differentiability, integrability.

MATH 868 - Real Analysis II
Credits: 3
Theory of integration; series; power series and uniform convergence of power series.

MATH #869 - Introduction to Differential Geometry
Credits: 3
Introduction to the study of the geometric properties of curves and surfaces in 3-dimensional space.

MATH 870 - Foundations of Number Theory
Credits: 3
Factorization and prime numbers, arithmetic functions, congruences, reciprocity laws, quadratic forms, Diophantine equations, computational number theory. Offered in alternate years.

MATH 872 - Combinatorics
Credits: 3
Graph theory (including planar graphs, graph coloring, Hamiltonian circuits, trees); counting principles (including permutations, combinations, pigeonhole principle, inclusion-exclusion principle); and related topics.

MATH 876 - Logic
Credits: 3
Induction and recursion; sentential logic; first-order logic; completeness, consistency, and decidability, recursive function. (Not offered every year.)

MATH 883 - Set Theory
Credits: 3
Axiomatic set theory, including its history, Zermelo-Fraenkel axioms, ordinal and cardinal numbers, consistency, independence, and undecidability. (Not offered every year.)

MATH 884 - Topology
Credits: 3
Open sets, closure, base, and continuous functions. Connectedness, compactness, separation axioms, and metrizability.

MATH 888 - Complex Analysis
Credits: 3
Complex functions, sequences, limits, differentiability and Cauchy-Riemann equations, elementary functions, Cauchy's theorem and formula, Taylor's and Laurent's series, residues, conformal mapping.
Prerequisite(s): MATH 867 with a minimum grade of B-.
MATH 896 - Topics in Mathematics and Statistics  
Credits: 1-4  
New or specialized courses not covered in regular course offerings.  
Repeat Rule: May be repeated for a maximum of 99 credits.

MATH 898 - Master's Project  
Credits: 1-6  
May be repeated to a maximum of 6 credits. IA (continuous grading). Cr/F.  
Repeat Rule: May be repeated for a maximum of 6 credits.

MATH 900 - Bridges from the Classroom to Mathematics  
Credits: 1  
An introduction to the goals of the MST program. Students have the opportunity to explore mathematical problems; to complete activities that make connections between several areas of mathematics, including the mathematical content in the MST degree program and the secondary school mathematics classroom; and to participate in readings/on-line discussion on the nature of mathematics. Permission required. Cr/F.

MATH 902 - Classroom Mathematics Practicum  
Credits: 1  
A follow-up course to the six core mathematics content courses of the MST degree program. During the course, students choose a mathematical topic and/or set of concepts learned in one of the core MST courses and develop and teach a unit based on these concepts at the middle school or secondary school level. Permission required. Cr/F.  
Repeat Rule: May be repeated up to 3 times.

MATH 905 - Euclidean and non-Euclidean Geometries from a Synthetic Perspective  
Credits: 3  
An axiomatic development of geometry, beginning with finite geometries; emphasis is given to the fundamental concepts of Euclidean and non-Euclidean geometries from a synthetic perspective. Permission required.

MATH 906 - Analytic and Transformational Geometry  
Credits: 3  
Fundamental concepts of transformational, projective geometry, and inversive geometry, including properties of conics and quadratic surfaces. Permission required.

MATH 909 - Probability and Statistics for Teachers  
Credits: 3  
Permutations and combinations; finite sample spaces; random variables; binomial distributions; statistical applications.

MATH #910 - Selected Topics in Mathematics Education for Teachers  
Credits: 1-4  
Current developments and issues in mathematics education; content, curricula, methods, and psychology of teaching mathematics. Can be repeated for credit.

MATH 913 - Graph Theory and Topics in Discrete Mathematics  
Credits: 3  
Key theoretical and computational aspects of graph theory and related areas of discrete mathematics. Applications of graph theory as well as current "open" problems are explored. Permission required.

MATH #914 - Topology for Teachers  
Credits: 3  
Fundamental concepts of elementary topology; network and map problems; sets, spaces, and transformations.

MATH 915 - Algebraic Structures  
Credits: 3  
An exploration of the structural similarities between and among seemingly disparate number systems, beginning with counting numbers, and progressing to integers, the rational numbers, the real numbers, and the complex numbers; and leading to a discussion of polynomials as an integer analogue and to fields as polynomial "quotients" through the basic concepts of splitting fields and Galois Theory. Permission required.

MATH 916 - Theory of Numbers for Teachers  
Credits: 3  
Divisibility and primes; congruences; quadratic reciprocity; number theoretic functions; Diophantine equations; perfect and amicable numbers.

MATH #917 - Mathematical Proof and Problem Solving  
Credits: 1-3  
Introduction to abstract mathematics with an emphasis on problem solving and proof structure, methods and techniques. Content includes logic, set theory and basic number theory.

MATH 918 - Analysis of Real Numbers  
Credits: 3  
An introduction to the fundamental concepts in real analysis that provide the mathematical foundation for calculus. Content focuses on properties of sequences and series; properties of functions, including continuity, the derivative and the Riemann integral. Permission required.

MATH 925 - Problem Solving Seminar  
Credits: 3  
A study of variety of problem solving strategies and techniques in the context of solving mathematical problems. Problems will emphasize the connections between the core areas of algebra, geometry and analysis. Other mathematical topics may be included. Typically taken in conjunction with the Concluding Experience Problem Set. Cr/F.

MATH 928 - Selected Topics in Mathematics for Teachers  
Credits: 1-3  
New or specialized topics not covered in the regular course offerings. May be repeated for credit.

MATH 929 - Directed Reading  
Credits: 1-3  
A directed reading project on a selected topic in mathematics or mathematics education, planned in collaboration with a faculty member.  
Repeat Rule: May be repeated for a maximum of 6 credits.

MATH 931 - Mathematical Physics  
Credits: 3  
Complex variables, differential equations, asymptotic methods, integral transforms, special functions, linear vector spaces and matrices, Green's functions, and additional topics selected from integral equations, variational methods, numerical methods, tensor analysis, and group theory. Students are required to have a mastery of differential equations; linear algebra; multidimensional calculus.  
Equivalent(s): PHYS 931
MATH 941 - Bayesian and Computational Statistics
Credits: 3
Current approaches to Bayesian modeling and data analysis and related statistical methodology based on computational simulation. Fundamentals of Bayesian estimation and hypothesis testing. Multi-level and hierarchical Bayesian modeling for correlated data. Introduction to Markov chain Monte Carlo based estimation approaches such as the Gibbs sampler and the Metropolis-Hastings algorithm. Mastery of intermediate statistics is required for this course, including: distributions, discrete and continuous random variables, transformation of variables (calculus based), bivariate and multivariate normal distribution, maximum likelihood estimation; working knowledge of linear regression and analysis of variance; basic linear algebra: vectors and matrices, linear spaces, matrix multiplication, inverse of a matrix, positive definiteness. Matrix-vector notation for linear regression and ANOVA.

MATH 944 - Spatial Statistics
Credits: 3

MATH 945 - Advanced Theory of Statistics I
Credits: 3
Prerequisite(s): MATH 856 with a minimum grade of B-.

MATH 946 - Advanced Theory of Statistics II
Credits: 3

MATH 951 - Algebra I
Credits: 3
Groups and their homomorphisms, products and sums, structure of groups; rings and their homomorphisms, ideals, factorization properties.
Prerequisite(s): MATH 861 with a minimum grade of B-.

MATH 952 - Algebra II
Credits: 3
Field extensions; Galois theory; module theory.
Prerequisite(s): MATH 951 with a minimum grade of B-.

MATH 953 - Analysis I
Credits: 3
Measurable spaces and functions, measures, Lebesgue integrals, convergence theorems.
Prerequisite(s): MATH 867 with a minimum grade of B-.

MATH 954 - Analysis II
Credits: 3
Cauchy theory and local properties of analytic functions, Riemann mapping theorem, representation theorems, harmonic functions.
Prerequisite(s): MATH 888 with a minimum grade of B-.

MATH 955 - Topology I
Credits: 3
Subspace, product, and quotient topologies; embedding; separation and countability axioms; connectedness; compactness and compactifications; paracompactness, metrization, and metric completions.
Prerequisite(s): MATH 884 with a minimum grade of B-.

MATH 956 - Topology II
Credits: 3
Chain complexes; homology of simplicial complexes, singular homology and cohomology; axiomatic homology; cup and cap products.
Prerequisite(s): MATH 861 with a minimum grade of B- and MATH 884 with a minimum grade of B-.

MATH 958 - Foundations of Math Education
Credits: 1
Topics include: major issues and trends in mathematics education research, the profession and infrastructure of mathematics education, theoretical perspectives, cultural and historical aspects of mathematics education, and the research-practice interface. Examples span the K-16 spectrum.

MATH 959 - Introduction to Research Design in STEM Education
Credits: 3
This course provides an overview of research design including preliminary considerations that go into selecting a qualitative, quantitative, or mixed methods design. Topics include the definition of the various approaches, developing research questions and/or hypotheses, reviewing the literature, understanding the use of theory, anticipating ethical issues, and developing writing strategies.

MATH 966 - Topics in Algebraic Topology I
Credits: 3
An introduction to topics in algebraic topology.
Prerequisite(s): MATH #956 with a minimum grade of B-.
Repeat Rule: May be repeated for a maximum of 99 credits.
MATH 968 - Topics in Mathematics Education I  
Credits: 3  
A) The Teaching and Learning of Mathematics; B) Curriculum and History in Mathematics Education. Topics selected from: epistemologies of knowledge applied to mathematics; theories of learning and teaching mathematics; theoretical perspectives in research; mathematics education research programs K-16; research methods for studying mathematics teaching, learning, and curricula; theoretical frameworks for curriculum development, implementation of new curricula, and research on curricula; historical perspectives of research in mathematics education; the evolution and history of K-16 mathematics curricula both in United States and internationally. Versions A and B offered alternately.  
Prerequisite(s): MATH 958 with a minimum grade of B-.  
Repeat Rule: May be repeated for a maximum of 99 credits.

MATH #969 - Topics in Probability and Statistics I  
Credits: 3  
Selected advanced topics from one or several of the following areas: probability, stochastic processes, design of experiments, biostatistics, Bayesian theory and methods, spatial and spatio-temporal statistics, time series analysis, nonparametric statistics.  
Repeat Rule: May be repeated for a maximum of 99 credits.

MATH 973 - Topics in Operator Theory  
Credits: 3  
Selected topics in operator theory.  
Prerequisite(s): MATH 863 with a minimum grade of B-.  
Repeat Rule: May be repeated for a maximum of 99 credits.

MATH 978 - Topics in Mathematics Education II  
Credits: 1-3  
An exploration of an area of research in mathematics education.  
Repeat Rule: May be repeated for a maximum of 99 credits.

MATH 979 - Research Topics in Statistics  
Credits: 3  
An exploration of the main statistical issues and computational methods associated with research problems from such areas as survival analysis, reliability, latitudinal data, categorical data, spatio-temporal data, and industrial processes. Student term projects require: literature searches, presentation, use of modern statistical software, and written reports. May be repeated barring duplication of topic.  
Repeat Rule: May be repeated up to unlimited times.

MATH 997 - Statistics Seminar  
Credits: 1  
A seminar of weekly and bi-weekly meetings organized by the statistics Ph.D. students with supervision by a statistics faculty member. Informal presentations of faculty members, students, and outside guest presenters; also discussion of topics that are of mutual interest to its participants. Dissertation proposal presentations. Seminar presentations are open to the greater public. Statistics Ph.D. students are required to enroll for at least 3 semesters. Attendance is mandatory by those students who are enrolled in the seminar. Credits do not count towards the Master’s degree. Cr/F.  
Repeat Rule: May be repeated for a maximum of 6 credits.

MATH 998 - Reading Courses  
Credits: 1-6  

MATH 999 - Doctoral Research  
Credits: 0  
Cr/F.